

RULES

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(cx) = c$$

$$\frac{d}{dx}(c) = 0$$

$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$1. f(x) = \sqrt[3]{x}$$

$$= x^{\frac{1}{3}}$$

$$f'(x) = \frac{1}{3} x^{\frac{1}{3}-1}$$

$$= \frac{1}{3} x^{-\frac{2}{3}}$$

$$= \boxed{\frac{1}{3x^{2/3}}}$$

$$2. f(x) = 5x^3 - 7x^2 + 4x - 1$$

$$f'(x) = 5 \cdot 3x^{3-1} - 7 \cdot 2x^{2-1} + 4 + 0$$

$$= \boxed{15x^2 - 14x + 4}$$

$$3. f(x) = \frac{1}{5}e^x + 4 \cos x$$

$$f'(x) = \frac{1}{5}e^x + 4(-\sin x)$$

$$= \boxed{\frac{1}{5}e^x - 4 \sin x}$$

$$4. f(x) = \frac{2}{5x^3}$$

$$= \frac{2x^{-3}}{5}$$

$$= \frac{2}{5}x^{-3}$$

$$f'(x) = \frac{2}{5}(-3)x^{-3-1}$$

$$= -\frac{6}{5}x^{-4}$$

$$= \boxed{-\frac{6}{5x^4}}$$

$$5. f(x) = \frac{\sqrt[5]{x}}{x^2}$$

$$= \frac{x^{\frac{1}{5}}}{x^2}$$

$$= x^{\frac{1}{5}-2}$$

$$= x^{-\frac{9}{5}}$$

$$f'(x) = -\frac{9}{5}x^{-\frac{9}{5}-1}$$

$$\rightarrow f'(x) = -\frac{9}{5}x^{-\frac{14}{5}}$$

$$= \boxed{\frac{-9}{5x^{14/5}}}$$