

$$1. f(x) = \frac{5}{6}x^3 - x^2 + 3x - 1$$

## FINDING INTERVALS OF CONCAVITY

① FIND SECOND DERIVATIVE

$$f'(x) = \frac{5}{6} \cdot 3x^2 - 2x + 3$$

$$f''(x) = \frac{5}{2}x^2 - 2x + 3$$

$$f'''(x) = \frac{5}{2} \cdot 2x - 2$$

$$f''(x) = 5x - 2 \leftarrow$$

② SET THIS EQUAL TO ZERO AND SOLVE

$$5x - 2 = 0$$



$$5x = 2$$

$$\frac{5x}{5} = \frac{2}{5}$$

$$x = \frac{2}{5} \leftarrow$$

CRITICAL NUMBERS

③ USING CRITICAL NUMBERS BUILD A TABLE OF INTERVALS, PICK TEST CASES, PLUG THEM INTO 2ND DERIVATIVE AND DETERMINE ANSWER

$-\infty$	$x = \frac{2}{5}$	$\infty$
$x=0$	$x=1$	TEST CASES
$5x-2$	$5x-2$	
$5(0)-2$	$5(1)-2$	
NEG.	POS.	
		

NOTE: IF SIGN IS NEG: CONCAVE DOWN  
IF SIGN IS POS: CONCAVE UP

CONC DOWN  $(-\infty, \frac{2}{5})$

CONC UP  $(\frac{2}{5}, \infty)$