

3. $f(x) = x + \frac{1}{\cos x}$ $0 \leq x < 2\pi$

① $f(x) = x + (\cos x)^{-1}$

$$f'(x) = 1 - 1(\cos x)^{-2} \cdot \frac{d}{dx}(\cos x)$$

$$= 1 - (\cos x)^{-2} \cdot (-\sin x)$$

$$= 1 + \frac{\sin x}{(\cos x)^2}$$

$P = \cos x$ $Q = (\cos x)^{-1} \cdot \frac{d}{dx}(\cos x)$

$$= \frac{d}{dx}(\cos x)$$

$$= -\sin x$$

$$\frac{P'Q - PQ'}{Q^2}$$

$$f''(x) = \frac{\cos x \cos^2 x - \sin x (-2 \cos x \sin x)}{[(\cos x)^2]^2}$$

$$= \frac{\cos^3 x + 2 \cos x \sin^2 x}{\cos^4 x}$$

$$= \frac{\cos x [\cos^2 x + 2 \sin^2 x]}{\cos^4 x}$$

$$f''(x) = \frac{\cos^3 x + 2 \sin^2 x}{\cos^3 x}$$

②

$$\cos^2 x + 2 \sin^2 x = 0$$

$$1 - \sin^2 x + 2 \sin^2 x = 0$$

$$1 + \sin^2 x = 0$$

$$\sin^2 x = -1$$

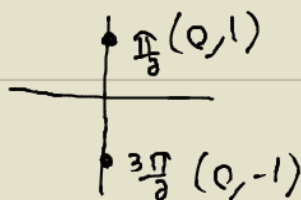
$$\sin x = \pm \sqrt{-1}$$

$$\cos^3 x = 0$$

$$[\cos x]^3 = 0$$

$$\cos x = 0$$

$$x = \frac{\pi}{2}, \frac{3\pi}{2}$$



③

$x=0$ $x=\frac{\pi}{2}$ $x=\frac{3\pi}{2}$ $x=2\pi$

| | | |
|---------------------------------|---------------------------------|---------------------------------|
| $x = \frac{\pi}{4}$ | $x = \pi$ | $x = \frac{7\pi}{4}$ |
| $\frac{\text{pos}}{[\cos x]^3}$ | $\frac{\text{pos}}{[\cos x]^3}$ | $\frac{\text{pos}}{[\cos x]^3}$ |
| pos | NEG | pos |
| ∪ | ∩ | ∪ |

conc up $(0, \frac{\pi}{2})$
 conc down $(\frac{\pi}{2}, \frac{3\pi}{2})$
 conc up $(\frac{3\pi}{2}, 2\pi)$