

$$5. y = 9 \arcsin \frac{x}{3} - x \sqrt{9-x^2}$$

$$y = 9 \arcsin \frac{x}{3} - \underbrace{x}_P \underbrace{(9-x^2)^{\frac{1}{2}}}_Q$$

$$P' = 1 \quad Q' = \frac{1}{2} (9-x^2)^{\frac{1}{2}-1} \cdot \frac{d}{dx} (9-x^2)$$

$$= \frac{1}{2} (9-x^2)^{-\frac{1}{2}} \cdot (-2x)$$

$$= \frac{-2x}{2(9-x^2)^{\frac{1}{2}}}$$

$$Q' = \frac{-x}{(9-x^2)^{\frac{1}{2}}}$$

$$P'Q + PQ'$$

$$y' = 9 \cdot \frac{1}{\sqrt{1-(\frac{x}{3})^2}} \cdot \frac{d}{dx} \left(\frac{x}{3}\right) - \left[ 1 \cdot (9-x^2)^{\frac{1}{2}} + x \left( \frac{-x}{(9-x^2)^{\frac{1}{2}}} \right) \right]$$

$$= \frac{9 \cdot \frac{1}{3}}{\sqrt{1-\frac{x^2}{9}}} - \left[ \frac{(9-x^2)^{\frac{1}{2}}}{1} - \frac{x^2}{(9-x^2)^{\frac{1}{2}}} \right]$$

$$= \frac{3}{\sqrt{\frac{9-x^2}{9}}} - \left[ \frac{(9-x^2)^{\frac{1}{2}}(9-x^2)^{\frac{1}{2}}}{(9-x^2)^{\frac{1}{2}}} - \frac{x^2}{(9-x^2)^{\frac{1}{2}}} \right]$$

$$= \frac{3}{\sqrt{\frac{9-x^2}{9}}} - \left[ \frac{9-x^2-x^2}{(9-x^2)^{\frac{1}{2}}} \right]$$

$$= \frac{3}{\frac{\sqrt{9-x^2}}{\sqrt{9}}} - \frac{9-2x^2}{(9-x^2)^{\frac{1}{2}}}$$

$$= \frac{3}{\frac{\sqrt{9-x^2}}{3}} - \frac{9-2x^2}{\sqrt{9-x^2}}$$

$$3 \cdot \frac{3}{\sqrt{9-x^2}} - \frac{9-2x^2}{\sqrt{9-x^2}}$$

$$= \frac{9-9+2x^2}{\sqrt{9-x^2}}$$

$$= \boxed{\frac{2x^2}{\sqrt{9-x^2}}}$$