

$$19. f(x) = \sqrt{x-3}$$

$$f(\underline{x+\Delta x}) = \sqrt{(\underline{x+\Delta x}) - 3}$$
$$= \sqrt{x+\Delta x - 3}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{f(x+\Delta x) - f(x)}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{\sqrt{x+\Delta x - 3} - \sqrt{x-3}}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{\sqrt{x+\Delta x - 3} - \sqrt{x-3}}{\Delta x} \cdot \frac{\sqrt{x+\Delta x - 3} + \sqrt{x-3}}{\sqrt{x+\Delta x - 3} + \sqrt{x-3}}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{x + \Delta x - 3 - (x - 3)}{\Delta x (\sqrt{x+\Delta x - 3} + \sqrt{x-3})}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{\overset{\cdot}{x} + \overset{\Delta}{\Delta x} - \overset{\cdot}{3} - \overset{\cdot}{x} + \overset{\Delta}{3}}{\Delta x (\sqrt{x+\Delta x - 3} + \sqrt{x-3})}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{\cancel{\Delta x}}{\cancel{\Delta x} (\sqrt{x+\Delta x - 3} + \sqrt{x-3})}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{1}{\sqrt{x+\Delta x - 3} + \sqrt{x-3}}$$

$$= \frac{1}{\sqrt{x+0-3} + \sqrt{x-3}}$$

$$= \frac{1}{\sqrt{x-3} + \sqrt{x-3}}$$

$$= \boxed{\frac{1}{2\sqrt{x-3}}}$$