

14. $f(x) = \underbrace{x^2}_P \underbrace{e^{-x}}_Q$

① $P' = 2x$ $Q' = e^{-x} \cdot \frac{d}{dx}(-x)$
 $Q' = -e^{-x}$

$P'Q + PQ'$

$f'(x) = 2xe^{-x} + x^2(-e^{-x})$
 $= e^{-x}(2x - x^2)$

② $e^{-x}(2x - x^2) = 0$

$e^{-x} \cdot x(2-x) = 0$

~~$e^{-x} = 0$~~ $x=0$ $2-x=0$
 $2=x$

③

$-\infty$	$x=0$	$x=2$	∞
$x=-1$	$x=1$	$x=3$	
$x(2-x)$	$x(2-x)$	$x(2-x)$	
$- (+)$	$+ (+)$	$+ (-)$	
	REL MIN	REL MAX	

DEC $(-\infty, 0)$
 INC $(0, 2)$
 DEC $(2, \infty)$

④) REL MIN

$x=0$

$y = x^2 e^{-x}$

$y = 0^2 e^{-0}$

$y = 0$

REL MIN $(0, 0)$

REL MAX

$x=2$

$y = x^2 e^{-x}$

$y = 2^2 e^{-2}$

$y = \frac{4}{e^2}$

REL MAX $(2, \frac{4}{e^2})$