

$$23. \quad y = \cos x + \sin(2x) \quad 0 \leq x \leq \frac{\pi}{2}$$

$$\text{AREA} = \int_0^{\frac{\pi}{2}} (\cos x + \sin 2x) dx$$

$$= \int_0^{\frac{\pi}{2}} \cos x dx + \int_0^{\frac{\pi}{2}} \sin 2x dx$$

$u = 2x \quad du = 2 dx$

$$= [\sin x]_0^{\frac{\pi}{2}} + \frac{1}{2} \int_0^{\frac{\pi}{2}} \sin 2x dx$$

$$= \sin \frac{\pi}{2} - \sin 0 + \frac{1}{2} \int_{x=0}^{x=\frac{\pi}{2}} \sin u du$$

$$= 1 - 0 + \frac{1}{2} [-\cos u]_{x=0}^{x=\frac{\pi}{2}}$$

$$= 1 - \frac{1}{2} [\cos 2x]_0^{\frac{\pi}{2}}$$

$$= 1 - \frac{1}{2} [\cos 2 \cdot \frac{\pi}{2} - \cos 2 \cdot 0]$$

$$= 1 - \frac{1}{2} [-1 - 1]$$

$$= 1 - \frac{1}{2} (-2)$$

$$= 1 + 1$$

$$= \textcircled{2}$$