

$$9. \int \frac{x-5}{(x+2)^2+3} dx$$

$$u = (x+2)^2 + 3$$

$$du = 2(x+2)' dx$$

$$du = (2x+4) dx$$

$$= \frac{1}{2} \int \frac{2(x-5)}{(x+2)^2+3} dx$$

$$= \frac{1}{2} \int \frac{2x-10}{(x+2)^2+3} dx$$

$$= \frac{1}{2} \int \frac{2x+4-14}{(x+2)^2+3} dx$$

$$= \frac{1}{2} \int \frac{2x+4}{(x+2)^2+3} dx - \frac{1}{2} \int \frac{14}{(x+2)^2+3} dx$$

$$u = (x+2)^2+3$$

$$du = (2x+4) dx$$

$$= \frac{1}{2} \int \frac{1}{u} du - \frac{1}{2} \cdot 14 \int \frac{1}{(\sqrt{3})^2 + (x+2)^2} dx$$

$$a = \sqrt{3} \quad w = x+2 \quad dw = dx$$

$$= \frac{1}{2} \ln|u| - 7 \int \frac{1}{a^2+w^2} dw$$

$$= \frac{1}{2} \ln|(x+2)^2+3| - 7 \cdot \frac{1}{a} \arctan \frac{w}{a} + C$$

$$= \frac{1}{2} \ln((x+2)^2+3) - 7 \cdot \frac{1}{\sqrt{3}} \arctan \frac{x+2}{\sqrt{3}} + C$$