

$$10. \int \frac{x-1}{x^2+4x+5} dx$$

$$u = x^2 + 4x + 5 \\ du = (2x + 4) dx$$

$$= \int \frac{2x+4-5}{x^2+4x+5} dx$$

$$= \int \frac{2x+4}{x^2+4x+5} dx - \int \frac{5}{x^2+4x+5} dx$$

$$u = x^2 + 4x + 5 \\ du = (2x + 4) dx$$

$$(4 \cdot \frac{1}{2})^2 \\ \frac{(2)^2}{4}$$

$$= \int \frac{1}{u} du - \int \frac{5}{x^2+4x+4-4+5} dx$$

$$= \ln|u| - 5 \int \frac{1}{(x+2)^2 + 1} dx$$

$$= \ln|x^2+4x+5| - 5 \int \frac{1}{(1)^2 + (x+2)^2} dx$$

$$a=1 \quad u=x+2 \quad du=dx$$

$$= \ln|x^2+4x+5| - 5 \int \frac{1}{a^2+u^2} du$$

$$= \ln|x^2+4x+5| - 5 \cdot \frac{1}{a} \arctan \frac{u}{a} + C$$

$$= \ln|x^2+4x+5| - 5 \cdot \frac{1}{1} \arctan \frac{x+2}{1} + C$$

$$= \ln|x^2+4x+5| - 5 \arctan(x+2) + C$$