

$$8. \lim_{\substack{x \rightarrow 4 \\ c}} \underbrace{(2x+1)}_{f(x)} = \underbrace{9}_L$$

$$|f(x) - L| < \epsilon \quad \text{WHEN} \quad 0 < |x - c| < \delta$$

$$|2x+1 - 9| < \epsilon \quad \text{WHEN} \quad 0 < \underline{|x-4|} < \underline{\delta}$$

$$\epsilon > |8-2x|$$

$$\epsilon > |4-x|\epsilon$$

$$\frac{\epsilon}{2} > |4-x|$$

$$\underline{|x-4|} < \underline{\frac{\epsilon}{2}} \quad \text{so} \quad \delta = \frac{\epsilon}{2}$$

$$|x-c| < \delta$$

$$|x-4| < \frac{\epsilon}{2}$$

$$\left(\frac{\epsilon}{2}\right)\epsilon > |4-x|\epsilon$$

$$\epsilon > |8-2x|$$

$$\epsilon > |6-1+x|$$

$$|f(x) - L| < \epsilon \quad \checkmark$$