

$$8. f(x) = 2x^5 \left(2 + \frac{3}{x-1} \right)$$

$$3 \frac{1}{2} = \frac{7}{2}$$

$$= 2x^5 \left(\frac{2(x-1)+3}{x-1} \right)$$

$$= 2x^5 \left(\frac{2x-2+3}{x-1} \right)$$

$$= 2x^5 \left(\frac{2x+1}{x-1} \right)$$

$$= \frac{4x^6 + 2x^5}{x-1} \quad \begin{matrix} P \\ Q \end{matrix}$$

$$P' = 24x^5 + 10x^4$$

$$Q' = 1$$

$$\frac{P'Q - PQ'}{Q^2}$$

$$f'(x) = \frac{(24x^5 + 10x^4)(x-1) - (4x^6 + 2x^5)(1)}{(x-1)^2}$$

$$= \frac{2x^4(12x+5)(x-1) - 2x^5(2x+1)}{(x-1)^2}$$

$$= \frac{2x^4 [(12x+5)(x-1) - x(2x+1)]}{(x-1)^2}$$

$$= \frac{2x^4 [12x^2 - 12x + 5x - 5 - 2x^2 - x]}{(x-1)^2}$$

$$= \frac{2x^4 (10x^2 - 8x - 5)}{(x-1)^2}$$