

$$15. f(x) = \underbrace{\tan x}_P [\underbrace{\sin x - \cos x}_Q] \quad \left(\frac{\pi}{4}, 0 \right)$$

$$\textcircled{1} \quad P' = \sec^2 x \quad Q' = \cos x - (-\sin x) \\ = \cos x + \sin x$$

$$P'Q + PQ'$$

$$f'(x) = \sec^2 x (\sin x - \cos x) + \tan x (\cos x + \sin x)$$

$$\textcircled{2} \quad m = \underbrace{\sec^2 \left(\frac{\pi}{4} \right)}_{\frac{1}{x}} \left(\sin \frac{\pi}{4} - \cos \frac{\pi}{4} \right) + \underbrace{\tan \frac{\pi}{4}}_{\frac{y}{x}} \left(\cos \frac{\pi}{4} + \sin \frac{\pi}{4} \right)$$

$$m = \left(\frac{1}{\frac{\sqrt{2}}{2}} \right)^2 \left(\frac{\sqrt{2}}{2} - \frac{\sqrt{2}}{2} \right) + \left(\frac{\frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} \right) \left(\frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2} \right)$$

$$m = 1 \left(\frac{2\sqrt{2}}{2} \right)$$

$$\boxed{m = \sqrt{2}}$$

