

$$19. f(x) = 2x + 5x^{-3}$$

$$f'(x) = 2 + 5(-3)x^{-4} \\ = 2 - 15x^{-4}$$

$$f''(x) = -15(-4)x^{-5} \\ = 60x^{-5} \\ = \frac{60}{x^5}$$

$$20. f(x) = \csc x$$

$$f'(x) = \underbrace{-\csc x}_P \underbrace{\cot x}_Q$$

$$P' = -(-\csc x \cot x) \quad Q' = -\csc^2 x$$

$$P'Q + PQ'$$

$$f''(x) = \csc x \cot x \cot x + (-\csc x)(-\csc^2 x)$$

$$= \csc x [\cot^2 x + \csc^2 x]$$

$$= \csc x [\csc^2 x - 1 + \csc^2 x]$$

$$= \csc x [2\csc^2 x - 1]$$

$$\sin^2 x + \cos^2 x = 1$$

$$\tan^2 x + 1 = \sec^2 x$$

$$\rightarrow 1 + \cot^2 x = \csc^2 x$$

$$1 = \csc^2 x - \cot^2 x$$

$$\cot^2 x = \csc^2 x - 1$$