

$$\frac{d}{dx}(\ln x) = \frac{1}{x}$$

$$\frac{d}{dx}(\ln u) = \frac{1}{u} \cdot u'$$

$$8. h(x) = \ln(3x^2 - 7x + 1)$$

$$h'(x) = \frac{1}{3x^2 - 7x + 1} \cdot \frac{d}{dx}(3x^2 - 7x + 1)$$

$$= \frac{1}{3x^2 - 7x + 1} \cdot (6x - 7)$$

$$= \boxed{\frac{6x - 7}{3x^2 - 7x + 1}}$$

$$9. h(x) = \ln \sqrt[5]{x^2 + 3}$$

$$h(x) = \ln (x^2 + 3)^{\frac{1}{5}}$$

$$h(x) = \frac{1}{5} \ln(x^2 + 3)$$

$$h'(x) = \frac{1}{5} \cdot \frac{1}{x^2 + 3} \cdot \frac{d}{dx}(x^2 + 3)$$

$$= \frac{1}{5} \cdot \frac{1}{x^2 + 3} \cdot 2x$$

$$= \boxed{\frac{2x}{5(x^2 + 3)}}$$

$$10. h(x) = \ln \sqrt[7]{\frac{3x-1}{x+4}}$$

$$= \ln \left(\frac{3x-1}{x+4} \right)^{\frac{1}{7}}$$

$$= \frac{1}{7} \ln \left(\frac{3x-1}{x+4} \right)$$

$$= \frac{1}{7} \ln(3x-1) - \frac{1}{7} \ln(x+4)$$

$$h'(x) = \frac{1}{7} \cdot \frac{1}{3x-1} \cdot \frac{d}{dx}(3x-1) - \frac{1}{7} \cdot \frac{1}{x+4} \cdot \frac{d}{dx}(x+4)$$

$$= \frac{1}{7} \cdot \frac{1}{3x-1} \cdot 3 - \frac{1}{7} \cdot \frac{1}{x+4} \cdot 1$$

$$= \frac{3}{7(3x-1)} - \frac{1}{7(x+4)}$$

$$= \frac{3(x+4)}{7(3x-1)(x+4)} - \frac{1(3x-1)}{7(3x-1)(x+4)}$$

$$= \frac{3x+12}{7(3x-1)(x+4)} - \frac{3x-1}{7(3x-1)(x+4)}$$

$$= \frac{3x+12-3x+1}{7(3x-1)(x+4)}$$

$$= \boxed{\frac{13}{7(3x-1)(x+4)}}$$