

1. $f(x) = 3 - x^2$

FINDING DERIVATIVE

① FIND $f(x)$

$$f(x) = 3 - x^2$$

② FIND $f(x + \Delta x)$

$$f(x + \Delta x) = 3 - (x + \Delta x)^2$$

$$= 3 - (x + \Delta x)(x + \Delta x)$$

$$= 3 - (x^2 + x\Delta x + x\Delta x + (\Delta x)^2)$$

$$= 3 - (x^2 + 2x\Delta x + (\Delta x)^2)$$

$$= 3 - x^2 - 2x\Delta x - (\Delta x)^2$$

③ PLUG IN $f(x)$ AND $f(x + \Delta x)$ INTO FORMULA AND FIND LIMIT

$$f'(x) = \lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{3 - x^2 - 2x\Delta x - (\Delta x)^2 - (3 - x^2)}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{\overset{0}{3} - \overset{0}{x^2} - 2x\Delta x - (\Delta x)^2 - \overset{0}{3} + \overset{0}{x^2}}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{-2x\Delta x - (\Delta x)^2}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{\cancel{\Delta x}(-2x - \Delta x)}{\cancel{\Delta x}}$$

$$= \lim_{\Delta x \rightarrow 0} -2x - \Delta x$$

$$= -2x - 0$$

$$= \boxed{-2x}$$

DERIVATIVE

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$