

$$3. f(x) = \sqrt{x-a}$$

$$\textcircled{1} f(x) = \sqrt{x-a}$$

$$\textcircled{2} f(\underline{x+h}) = \sqrt{\underline{(x+h)} - a}$$
$$= \sqrt{x+h-a}$$

$$\textcircled{3} f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$
$$= \lim_{h \rightarrow 0} \frac{\sqrt{x+h-a} - \sqrt{x-a}}{h}$$
$$= \lim_{h \rightarrow 0} \frac{\sqrt{x+h-a} - \sqrt{x-a}}{h} \cdot \frac{\sqrt{x+h-a} + \sqrt{x-a}}{\sqrt{x+h-a} + \sqrt{x-a}}$$
$$= \lim_{h \rightarrow 0} \frac{x+h-a - (x-a)}{h(\sqrt{x+h-a} + \sqrt{x-a})}$$
$$= \lim_{h \rightarrow 0} \frac{\overset{\square}{x+h-a} - \overset{\square}{x-a}}{h(\sqrt{x+h-a} + \sqrt{x-a})}$$
$$= \lim_{h \rightarrow 0} \frac{\overset{\color{red}{\cancel{h}}}}{\overset{\color{red}{\cancel{h}}}{h}(\sqrt{x+h-a} + \sqrt{x-a})}$$
$$= \lim_{h \rightarrow 0} \frac{1}{\sqrt{x+h-a} + \sqrt{x-a}}$$
$$= \frac{1}{\sqrt{x+0-a} + \sqrt{x-a}}$$
$$= \boxed{\frac{1}{2\sqrt{x-a}}}$$