Concavity and the Second Derivative Test

In problems 1-4, Determine the open intervals on which the graph of the function is concave upward or concave downward.

| 1. $f(x) = -7x^2 - 3x + 2$ | $2. \ \ f(x) = 2x^3 - 4x^2 - 3$ |
|--------------------------------|---------------------------------|
| 3. $f(x) = \frac{2x}{x^2 + 1}$ | 4. $f(x) = \frac{x+3}{x-2}$ |

In problems 5-8, Discuss the concavity of the graph of the function and find the points of inflection.

| 5. $f(x) = x^3 - 21x^2 + 18x - 6$ | 6. $f(x) = x^4 + 4x^3 - 18x^2 + 12x - 48$ |
|-----------------------------------|---|
| 7. $f(x) = x^4 + 3x^2$ | 8. $f(x) = 5x(3-x)^2$ |

In problems 9-11, Find all relative extrema of the function. Use the Second-Derivative Test when applicable.

| 9. $f(x) = x^2 - 8x + 2$ | 10. $f(x) = 2x^3 - 21x^2 + 60x + 12$ |
|--------------------------|--------------------------------------|
| 11. $f(x) = x^{1/3} - 4$ | |

In problems 12-13, Find all relative extrema and points of inflection.

12.
$$f(x) = -x^3 + 3x$$
 13. $f(x) = x^4 - 4x^2 + 2$

14. Find the point of diminishing returns for the function R (revenue) and x is amount spent.

$$R = -x^3 + 6x^2 + 2$$

15. Find the point of diminishing returns for the function R (revenue) and x is amount spent

$$R = x^3 - 15x^2 + 12x - 6$$