

8. $z = 3xy$, $x^2 + y^2 = 4$, first octant

$$\int_{\theta=0}^{\theta=\frac{\pi}{2}} \int_{r=0}^{r=2} 3(r \cos \theta)(r \sin \theta) r \, dr \, d\theta$$

$$= 3 \int_{\theta=0}^{\theta=\frac{\pi}{2}} \int_{r=0}^{r=2} r^3 \cos \theta \sin \theta \, dr \, d\theta$$

$$= 3 \int_{\theta=0}^{\theta=\frac{\pi}{2}} \left[\frac{1}{4} r^4 \cos \theta \sin \theta \right]_{r=0}^{r=2} d\theta$$

$$= 3 \cdot \frac{1}{4} \int_{\theta=0}^{\theta=\frac{\pi}{2}} \cos \theta \sin \theta [r^4]_{r=0}^{r=2} d\theta$$

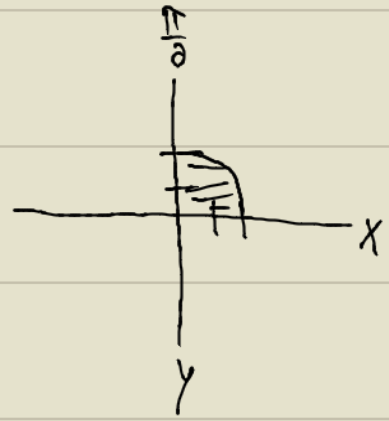
$$= \frac{3}{4} \int_{\theta=0}^{\theta=\frac{\pi}{2}} \cos \theta \sin \theta [2^4 - 0^4] d\theta$$

$$= \frac{3}{4} \cdot 16 \int_{\theta=0}^{\theta=\frac{\pi}{2}} \cos \theta \sin \theta \, d\theta$$

$$= 12 \int_{\theta=0}^{\theta=\frac{\pi}{2}} u \, du \quad u = \sin \theta \quad du = \cos \theta \, d\theta$$

$$= 12 \left[\frac{1}{2} u^2 \right]_{\theta=0}^{\theta=\frac{\pi}{2}}$$

$$= 12 \cdot \frac{1}{2} \left[\sin^2 \theta \right]_{\theta=0}^{\theta=\frac{\pi}{2}}$$



$$x = r \cos \theta$$

$$y = r \sin \theta$$

$$= 6 \left[\sin^2 \left(\frac{\pi}{2} \right) - \sin^2 (0) \right]$$

$$= 6 [1^2 - 0^2]$$

$$= \textcircled{6}$$