

## Divergence Theorem

## The Divergence Theorem

Let  $Q$  be a solid region bounded by a closed surface  $S$  oriented by a unit normal vector directed outward from  $Q$ . If  $\mathbf{F}$  is a vector field whose component functions have continuous first partial derivatives in  $Q$ , then:

$$\iint_S \mathbf{F} \cdot \mathbf{N} \, dS = \iiint_Q \operatorname{div} \mathbf{F} \, dV$$

1. Use the Divergence Theorem to evaluate the integral and find the outward flux of  $\mathbf{F}$  through the surface of the solid bounded by the graphs of the equations.

(Similar to p.1131 #7-18)

$$\iint_S \mathbf{F} \cdot \mathbf{N} \, dS$$

$$\mathbf{F}(x, y, z) = (2x^2)\mathbf{i} + (3y^2)\mathbf{j} + (z^2)\mathbf{k}$$

$$S : x = 0, x = 2, y = 0, y = 1, z = 0, z = 3$$

2. Use the Divergence Theorem to evaluate the integral and find the outward flux of  $\mathbf{F}$  through the surface of the solid bounded by the graphs of the equations.

(Similar to p.1131 #7-18)

$$\iint_S \mathbf{F} \cdot \mathbf{N} \, dS$$

$$\mathbf{F}(x, y, z) = (2x)\mathbf{i} + (2y)\mathbf{j} + (2z)\mathbf{k}$$

$$S : x^2 + y^2 + z^2 = 4$$

3. Use the Divergence Theorem to evaluate the integral and find the outward flux of  $\mathbf{F}$  through the surface of the solid bounded by the graphs of the equations.

(Similar to p.1131 #7-18)

$$\iint_S \mathbf{F} \cdot \mathbf{N} \, dS$$

$$\mathbf{F}(x, y, z) = (2x)\mathbf{i} + (y^2)\mathbf{j} + (2z)\mathbf{k}$$

$$S : x^2 + y^2 = 9, z = 0, z = 5$$

4. Use the Divergence Theorem to evaluate the integral and find the outward flux of  $\mathbf{F}$  through the surface of the solid bounded by the graphs of the equations.

(Similar to p.1131 #7-18)

$$\iint_S \mathbf{F} \cdot \mathbf{N} \, dS$$

$$\mathbf{F}(x, y, z) = (2x^3)\mathbf{i} + (5x^2y)\mathbf{j} + (e^{xy})\mathbf{k}$$

$$S : z = 5 - y, z = 0, x = 0, x = 2, y = 0$$