

$$14. \int_{x=0}^{x=6} \int_{y=\frac{x}{3}}^{y=2} dy dx$$

$$= \int_{x=0}^{x=6} \left[ y \right]_{y=\frac{x}{3}}^{y=2} dx$$

$$= \int_{x=0}^{x=6} \left( 2 - \frac{x}{3} \right) dx$$

$$= \left[ 2x - \frac{1}{3} \cdot \frac{1}{2} x^2 \right]_{x=0}^{x=6}$$

$$= \left[ 2x - \frac{1}{6} x^2 \right]_{x=0}^{x=6}$$

$$= 2(6) - \frac{1}{6}(6)^2 - \left( 2(0) - \frac{1}{6}(0)^2 \right)$$

$$= 12 - 6$$

$$= \boxed{6}$$

$$\int_{y=0}^{y=2} \int_{x=0}^{x=3y} dx dy$$

$$= \int_{y=0}^{y=2} \left[ x \right]_{x=0}^{x=3y} dy$$

$$= \int_{y=0}^{y=2} (3y - 0) dy$$

$$= \int_{y=0}^{y=2} (3y) dy$$

$$= \left[ \frac{3}{2} y^2 \right]_{y=0}^{y=2}$$

$$= \frac{3}{2}(2)^2 - \frac{3}{2}(0)^2$$

$$= \boxed{6}$$



$$y = \frac{x}{3}$$

$$3y = x$$