

$$5. \int_C (x^2 + y^2 - z) ds \quad C: \vec{r}(t) = (\sin t) \vec{i} + (\cos t) \vec{j} + 3\vec{k}$$

$$0 \leq t \leq \frac{\pi}{2} \quad x(t) = \sin t \quad y(t) = \cos t \quad z(t) = 3$$

$$f(x, y, z) = x^2 + y^2 - z$$

$$f(x(t), y(t), z(t)) = (\sin t)^2 + (\cos t)^2 - 3$$

$$= 1 - 3$$

$$= -2$$

$$\int_a^b f(x(t), y(t), z(t)) \sqrt{[x'(t)]^2 + [y'(t)]^2 + [z'(t)]^2} dt$$

$$\int_0^{\frac{\pi}{2}} (-2) \sqrt{(\cos t)^2 + (-\sin t)^2 + 0^2} dt$$

$$= -2 \int_0^{\frac{\pi}{2}} \sqrt{1} dt$$

$$= -2 \int_0^{\frac{\pi}{2}} 1 dt$$

$$= -2 [t]_0^{\frac{\pi}{2}}$$

$$= -2 \left[\frac{\pi}{2} - 0 \right]$$

$$= \boxed{-\pi}$$

$$x'(t) = \cos t$$

$$y'(t) = -\sin t$$

$$z'(t) = 0$$