

$$1. \iint_S (x-5y+z) \, dS \quad S: z = 10-x \quad 0 \leq x \leq 10 \quad 0 \leq y \leq 10$$

$$g(x,y) = 10-x$$

$$f(x,y,g(x,y)) = f(x,y,10-x) = x-5y+10-x = -5y+10$$

$\begin{matrix} \uparrow & \uparrow & \uparrow \\ x & y & z \end{matrix}$

$$g_x = -1 \quad g_y = 0$$

$$= \int_{x=0}^{x=10} \int_{y=0}^{y=10} (-5y+10) \sqrt{1+(-1)^2+0^2} \, dy \, dx$$

$$= \sqrt{2} \int_{x=0}^{x=10} \left[-\frac{5}{2}y^2 + 10y \right]_{y=0}^{y=10} \, dx$$

$$= \sqrt{2} \int_{x=0}^{x=10} \left[-\frac{5}{2}(10)^2 + 10(10) - \left(-\frac{5}{2}(0)^2 + 10(0) \right) \right] \, dx$$

$$= \sqrt{2} \int_{x=0}^{x=10} (-250 + 100) \, dx$$

$$= -150\sqrt{2} \int_{x=0}^{x=10} \, dx$$

$$= -150\sqrt{2} \left[x \right]_{x=0}^{x=10}$$

$$= -150\sqrt{2} [10 - 0]$$

$$= \boxed{-1500\sqrt{2}}$$