

$$3. \quad z = a - x - y$$

$$V = \int_{x=0}^{x=a} \int_{y=0}^{y=a-x} \int_{z=0}^{z=a-x-y} dz \, dy \, dx$$

$$= \int_{x=0}^{x=a} \int_{y=0}^{y=a-x} [z]_{z=0}^{z=a-x-y} dy \, dx$$

$$= \int_{x=0}^{x=a} \int_{y=0}^{y=a-x} (a-x-y-0) dy \, dx$$

$$= \int_{x=0}^{x=a} \int_{y=0}^{y=a-x} (a-x-y) dy \, dx$$

$$= \int_{x=0}^{x=a} \left[ay - xy - \frac{1}{2}y^2 \right]_{y=0}^{y=a-x} dx$$

$$= \int_{x=0}^{x=a} \left[a(a-x) - x(a-x) - \frac{1}{2}(a-x)^2 - (0) \right] dx$$

$$= \int_{x=0}^{x=a} \left(4 - 2x - 2x + x^2 - \frac{1}{2}(4 - 4x + x^2) \right) dx$$

$$= \int_{x=0}^{x=a} \left(4 - 4x + x^2 - 2 + 2x - \frac{1}{2}x^2 \right) dx$$

$$= \int_{x=0}^{x=a} \left(\frac{1}{2}x^2 - 2x + 2 \right) dx$$

$$= \left[\frac{1}{2} \cdot \frac{1}{3}x^3 - 2 \cdot \frac{1}{2}x^2 + 2x \right]_{x=0}^{x=a}$$

$$\frac{y's}{0 = a - x - y}$$

$$y = a - x$$

$$\frac{x's}{z = a - x - y}$$

$$0 = a - x - 0$$

$$x = a$$

$$= \left[\frac{1}{6}x^3 - x^2 + 2x \right]_{x=0}^{x=a}$$

$$= \frac{1}{6}(a)^3 - a^2 + 2(a) - \left(\frac{1}{6}(0)^3 - 0^2 + 2(0) \right)$$

$$= \frac{8}{6} - 4 + 4$$

$$= \left(\frac{4}{3} \right)$$