

5.  $z = 9 - x^2$ ,  $y = 9 - x^2$ , 1ST OCTANT

$$V = \int_{x=0}^{x=3} \int_{y=0}^{y=9-x^2} \int_{z=0}^{z=9-x^2} dz dy dx$$

$$= \int_{x=0}^{x=3} \int_{y=0}^{y=9-x^2} [z]_{z=0}^{z=9-x^2} dy dx$$

$$= \int_{x=0}^{x=3} \int_{y=0}^{y=9-x^2} (9-x^2-0) dy dx$$

$$= \int_{x=0}^{x=3} [(9-x^2)y]_{y=0}^{y=9-x^2} dx$$

$$= \int_{x=0}^{x=3} (9-x^2)[9-x^2-0] dx$$

$$= \int_{x=0}^{x=3} (81 - 9x^2 - 9x^2 + x^4) dx$$

$$= \int_{x=0}^{x=3} (81 - 18x^2 + x^4) dx$$

$$= \left[ 81x - 18 \cdot \frac{1}{3}x^3 + \frac{1}{5}x^5 \right]_{x=0}^{x=3}$$

$$= 81(3) - 6(3)^3 + \frac{1}{5}(3)^5 - \left( 81(0) - 6(0)^3 + \frac{1}{5}(0)^5 \right)$$

$$= 243 - 162 + \frac{243}{5}$$

$$= \frac{648}{5}$$

x's  
 $y = 9 - x^2$   
 $0 = 9 - x^2$   
 $x^2 = 9$   
 $x = \pm\sqrt{9}$   
 $x = \pm 3$