

#5

$$x^4 - x^3 + 3x^2 - 9x - 54 = 0$$

$x = -2$   
 $x = 3$

$$\begin{array}{r|rrrrr} -2 & 1 & -1 & 3 & -9 & -54 \\ & & -2 & 6 & -18 & 54 \\ \hline 3 & 1 & -3 & 9 & -27 & 0 \\ & & 3 & 0 & 27 & \\ \hline & 1 & 0 & 9 & 0 & \\ \hline & x^2 & x & mx & & \end{array}$$

$$x^2 = -9$$
  
$$x = \pm \sqrt{-9}$$
  
$$x = \pm 3i$$

$$x^2 + 9 = 0$$

#6

$$x^4 - 6x^3 + 30x^2 - 25 = 0$$

$x = 1$   
 $x = 5$

$$\begin{array}{r|rrrrr} 1 & 1 & -6 & 0 & 30 & -25 \\ & & 1 & -5 & -5 & 25 \\ \hline 5 & 1 & -5 & -5 & 25 & 0 \\ & & 5 & 0 & -25 & \\ \hline & 1 & 0 & -5 & 0 & \\ \hline & x^2 & x & mx & & \end{array}$$

$$x^2 = 5$$
  
$$x = \pm \sqrt{5}$$

$$x^2 - 5 = 0$$

#7

$$x^4 + 4x^3 + 6x^2 + 4x + 1 = 0$$

$x = -1$   
 $x = -1$

$$\begin{array}{r|rrrrr} -1 & 1 & 4 & 6 & 4 & 1 \\ & & -1 & -3 & -3 & -1 \\ \hline -1 & 1 & 3 & 3 & 1 & 0 \\ & & -1 & -2 & -1 & \\ \hline & 1 & 2 & 1 & 0 & \\ \hline & x^2 & x & mx & & \end{array}$$

$$x^2 + 2x + 1 = 0$$
  
$$(x+1)(x+1) = 0$$
  
$$x+1=0 \quad x+1=0$$
  
$$x = -1 \quad x = -1$$

#1 REVISITED

$$-x^3 - 3x^2 - 18x + 40 = 0$$
  
$$Q \quad P$$

P:  $\pm 1, \pm 2, \pm 4, \pm 5, \pm 8, \pm 10, \pm 20, \pm 40$   
Q:  $\pm 1$

$$\frac{P}{Q} = \pm 1, \pm 2, \pm 4, \pm 5, \pm 8, \pm 10, \pm 20, \pm 40$$

$$\begin{array}{r|rrrr} 1 & 1 & -3 & -18 & 40 \\ & & 1 & -21 & -20 \\ \hline & 1 & -2 & -20 & 20 \end{array} \quad \begin{array}{r|rrrr} 1 & 1 & -3 & -18 & 40 \\ & & -1 & 4 & 14 \\ \hline & 1 & -4 & -14 & 54 \end{array}$$

$$\begin{array}{r|rrrr} 2 & 1 & -3 & -18 & 40 \\ & & 2 & -24 & -40 \\ \hline & 1 & -1 & -20 & 0 \\ \hline & x^2 & x & mx & \end{array}$$

$$x^2 - x - 20 = 0$$
  
$$(x-5)(x+4) = 0$$
  
$$x-5=0 \quad x+4=0$$
  
$$x = 5 \quad x = -4$$