

QUADRATIC FORMULA

Form: $ax^2 + bx + c = 0$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

① $21x^2 + x - 2 = 0$

$a = 21 \quad b = 1 \quad c = -2$

$$x = \frac{-(1) \pm \sqrt{(1)^2 - 4(21)(-2)}}{2(21)}$$

$$= \frac{-1 \pm \sqrt{1 + 168}}{42}$$

$$= \frac{-1 \pm \sqrt{169}}{42}$$

$$= \frac{-1 \pm 13}{42}$$

$$x = \frac{-1 + 13}{42}$$

$$= \frac{12}{42}$$

$$= \frac{2}{7}$$

$$\frac{13}{13} \frac{39}{120} \frac{120}{169}$$

$$\frac{123}{x 57}$$

$$\frac{84}{2} \frac{84}{168}$$

$$x = \frac{-1 - 13}{42}$$

$$= \frac{-14}{42}$$

$$= \frac{-2}{6}$$

$$= \frac{-1}{3}$$

② $x + \frac{1}{x} = 5$

$$x + \frac{1}{x} - 5 = 0$$

$$x(x) + x(\frac{1}{x}) + x(-5) = 0$$

$$x^2 + 1 - 5x = 0$$

$$x^2 - 5x + 1 = 0$$

$a = 1 \quad b = -5 \quad c = 1$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-(-5) \pm \sqrt{(-5)^2 - 4(1)(1)}}{2(1)}$$

$$= \frac{5 \pm \sqrt{25 - 4}}{2}$$

$$= \frac{5 \pm \sqrt{21}}{2}$$

③ $7w^2 = -2w + 3$

$$7w^2 + 2w - 3 = 0$$

$a = 7 \quad b = 2 \quad c = -3$

$$w = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-2 \pm \sqrt{(2)^2 - 4(7)(-3)}}{2(7)}$$

$$= \frac{-2 \pm \sqrt{4 + 84}}{14}$$

$$= \frac{-2 \pm \sqrt{88}}{14}$$

$$= \frac{-2 \pm \sqrt{2 \cdot 2 \cdot 2 \cdot 11}}{14}$$

$$= \frac{-2 \pm 2\sqrt{22}}{14}$$

$$\frac{-1 \pm 1\sqrt{22}}{7}$$

$$\frac{-1 \pm \sqrt{22}}{7}$$

④ $3x^2 - 5x + 9 = 0$

$a = 3 \quad b = -5 \quad c = 9$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-(-5) \pm \sqrt{(-5)^2 - 4(3)(9)}}{2(3)}$$

$$= \frac{5 \pm \sqrt{25 - 108}}{6}$$

$$= \frac{5 \pm \sqrt{-83}}{6}$$

$$= \frac{5 \pm i\sqrt{83}}{6}$$

$$\frac{5}{6} \pm \frac{\sqrt{83}}{6}i$$