

The Cross Product

1. Find the value of each determinant  
(Similar to p.370 #7-10)

$$\begin{vmatrix} 2 & 5 \\ 8 & 3 \end{vmatrix}$$

2. Find the value of each determinant  
(Similar to p.370 #11-14)

$$\begin{vmatrix} A & B & C \\ 7 & -1 & 2 \\ 3 & -4 & -5 \end{vmatrix}$$

3. Find (a)  $\mathbf{v} \times \mathbf{w}$ , (b)  $\mathbf{w} \times \mathbf{v}$ , (c)  $\mathbf{w} \times \mathbf{w}$ ,  
and (d)  $\mathbf{v} \times \mathbf{v}$   
(Similar to p.370 #15-22)

$$\mathbf{v} = 3\mathbf{i} - 4\mathbf{j} + \mathbf{k}$$

$$\mathbf{w} = 2\mathbf{i} - 3\mathbf{j} + 5\mathbf{k}$$

4. Find (a)  $\mathbf{v} \times \mathbf{w}$ , (b)  $\mathbf{w} \times \mathbf{v}$ , (c)  $\mathbf{w} \times \mathbf{w}$ ,  
and (d)  $\mathbf{v} \times \mathbf{v}$   
(Similar to p.370 #15-22)

$$\mathbf{v} = \mathbf{i} + \mathbf{j} + \mathbf{k}$$

$$\mathbf{w} = 5\mathbf{i} - 2\mathbf{k}$$

5. Use the given vectors  $\mathbf{u}$ ,  $\mathbf{v}$ , and  $\mathbf{w}$  to  
find each expression.

$$\mathbf{u} = 3\mathbf{i} - \mathbf{j} + 2\mathbf{k} \quad \mathbf{v} = 4\mathbf{i} + \mathbf{j} - 5\mathbf{k}$$

$$\mathbf{w} = \mathbf{i} + \mathbf{j} + \mathbf{k}$$

(Similar to p.370 #23-40)

$$\mathbf{u} \times \mathbf{v}$$

6. Use the given vectors  $\mathbf{u}$ ,  $\mathbf{v}$ , and  $\mathbf{w}$  to find each expression.

$$\mathbf{u} = 3\mathbf{i} - \mathbf{j} + 2\mathbf{k} \quad \mathbf{v} = 4\mathbf{i} + \mathbf{j} - 5\mathbf{k}$$

$$\mathbf{w} = \mathbf{i} + \mathbf{j} + \mathbf{k}$$

(Similar to p.370 #23-40)

$$\mathbf{v} \times \mathbf{v}$$

7. Use the given vectors  $\mathbf{u}$ ,  $\mathbf{v}$ , and  $\mathbf{w}$  to find each expression.

$$\mathbf{u} = 3\mathbf{i} - \mathbf{j} + 2\mathbf{k} \quad \mathbf{v} = 4\mathbf{i} + \mathbf{j} - 5\mathbf{k}$$

$$\mathbf{w} = \mathbf{i} + \mathbf{j} + \mathbf{k}$$

(Similar to p.370 #23-40)

$$(-2\mathbf{v}) \times \mathbf{u}$$

8. Use the given vectors  $\mathbf{u}$ ,  $\mathbf{v}$ , and  $\mathbf{w}$  to find each expression.

$$\mathbf{u} = 3\mathbf{i} - \mathbf{j} + 2\mathbf{k} \quad \mathbf{v} = 4\mathbf{i} + \mathbf{j} - 5\mathbf{k}$$

$$\mathbf{w} = \mathbf{i} + \mathbf{j} + \mathbf{k}$$

(Similar to p.370 #23-40)

$$\mathbf{u} \cdot (\mathbf{w} \times \mathbf{v})$$

9. Use the given vectors  $\mathbf{u}$ ,  $\mathbf{v}$ , and  $\mathbf{w}$  to find each expression.

$$\mathbf{u} = 3\mathbf{i} - \mathbf{j} + 2\mathbf{k} \quad \mathbf{v} = 4\mathbf{i} + \mathbf{j} - 5\mathbf{k}$$

$$\mathbf{w} = \mathbf{i} + \mathbf{j} + \mathbf{k}$$

(Similar to p.370 #41-44)

vector orthogonal to both  $\mathbf{u}$  and  $\mathbf{v}$   
(Hint  $\mathbf{u} \times \mathbf{v}$  is orthogonal to both)

10. Find the area of the parallelogram with one corner at  $P_1$  and adjacent

sides  $\overrightarrow{P_1P_2}$  and  $\overrightarrow{P_1P_3}$

(Similar to p.370 #45-48)

$$P_1 = (-1, 0, 3), \quad P_2 = (3, 5, -4), \quad P_3 = (4, -1, 3)$$

Hint:  $\|\mathbf{u} \times \mathbf{v}\|$  is the area of the parallelogram where  $\mathbf{u}$  and  $\mathbf{v}$  are adjacent sides

11. Find the area of the parallelogram with vertices  $P_1$ ,  $P_2$ ,

$P_3$ , and  $P_4$

(Similar to p.370 #49-52)

$$P_1 = (4, 2, 3), \quad P_2 = (4, 3, 4),$$

$$P_3 = (0, -3, -1), \quad P_4 = (0, -2, 0)$$

Hint:  $\|\mathbf{u} \times \mathbf{v}\|$  is the area of the parallelogram where  $\mathbf{u}$  and  $\mathbf{v}$  are adjacent sides